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## Mathematical Modeling of the Effect of Titanium (Ti) Added as a Modifier on the Wear Resistance of a Low-Alloyed Steel Alloy

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**Abstract:** *This article presents a research analysis of the effect of the Ti element as a modifier on the wear resistance of the 35XGCL low – alloyed liquid steel alloy. Based on the obtained results, the increase in the number of crystallization centers of the cast alloy and the formation of a fine granular structure led to a significant increase in the wear resistance property of the cast product.*

**Keywords:** *modifier, wear resistance, low – alloyed, crystallization centers, Lagrange's interpolation polynomial, Cramer's method.*

**Introduction.** Today, the rolling machine shafts used in the stamping shops of production enterprises are the main and very expensive part of the machines for the production of rolled products. They faced various stresses and strains during their work. In addition, the geometric dimensions and material of the shafts must ensure that they can withstand the heaviest loads that occur during the shift sequence. Another important factor related to the service life of the shafts is the wear resistance of its material.

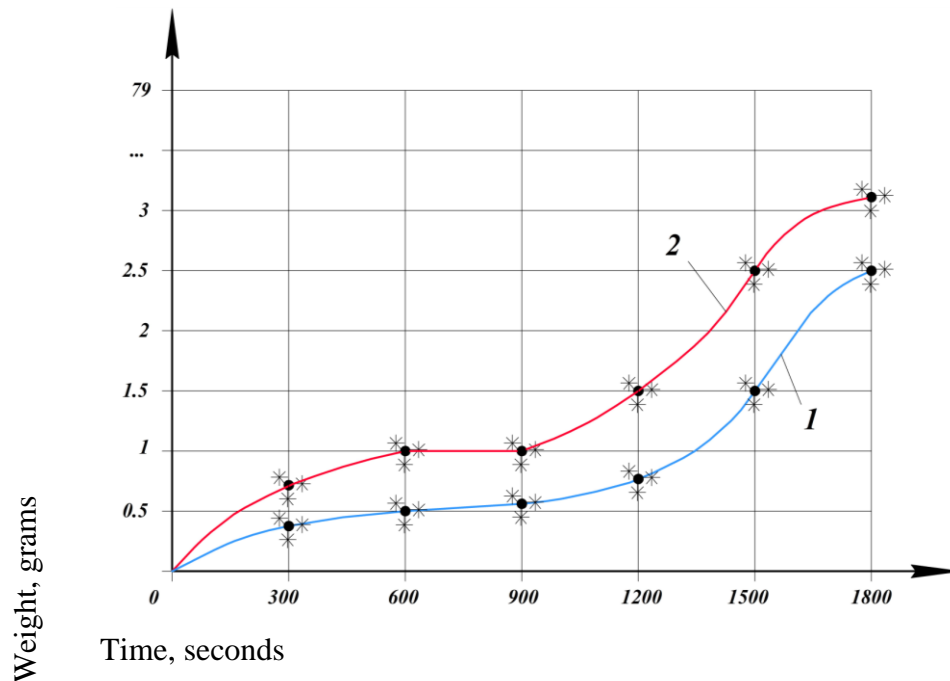
**Main part.** Wear resistance means the ability of a material to resist material loss as a result of some mechanical external influences.

This device can be used to determine the wear resistance of all types of metals. It's easy to use, with the option to control the speed of the diamond disc with automatic power-off at a selected number of revolutions. It is designed to carry out studies of special grinding disk speeds of 400, 525, 650, 775 and 900 revolutions per minute.



**Pic 1. General view of a special device with a diamond disc for determining the wear resistance of samples**

This graph presents the results of a study conducted to determine the effect of time-dependent corrosion resistance of research samples made from low-alloy steel alloys based on two types of composition [1 – 4].



**Pic 2. Wear resistance of research samples made of low – alloyed steel alloys as a function of time.**

1 – a sample containing 0.3-0.5% Ti element as a modifier in the composition of the alloy based on the given proposals; 2 – a sample cast from the 35XGCL brand at the production enterprise;

**Results.** Since the research was carried out on two types of alloys, we will formulate a mathematical expression of the wear resistance of both alloys.

First, we make a mathematical model of the wear resistance of a sample cast from a low – alloyed steel alloy of the 35XGCL brand, which was previously cast at the production plant. For this, time change is taken as a free variable, and we will consider the problem of creating a function that reflects the corrosion of the alloy. In this case, we construct Lagrange's interpolation polynomial, that is, by bringing the

problem into the system of algebraic equations, it is possible to express the function of the amount of consumption in the form of a polynomial by determining the unknown coefficients.

$m$  – wear resistance, gram;

$t$  – time, minute;

$$m = f(t); (1)$$

$$\begin{cases} 5^6 t_1 + 5^5 t_2 + \dots + 5 t_6 = 0.7 \\ 10^6 t_1 + 10^5 t_2 + \dots + 10 t_6 = 1 \\ 15^6 t_1 + 15^5 t_2 + \dots + 15 t_6 = 1 \\ 20^6 t_1 + 20^5 t_2 + \dots + 20 t_6 = 1.5 \\ 25^6 t_1 + 25^5 t_2 + \dots + 25 t_6 = 2.5 \\ 30^6 t_1 + 30^5 t_2 + \dots + 30 t_6 = 3.2 \end{cases}; \quad (2)$$

$$\begin{aligned} t_1 &= 1.3 \cdot 10^{-7}; \\ t_2 &= -1.4 \cdot 10^{-5}; \end{aligned}$$

$$\begin{aligned} t_3 &= 5.3 \cdot 10^{-4}; \\ t_4 &= -8.5 \cdot 10^{-3}; \end{aligned}$$

$$\begin{aligned} t_5 &= 0.05; \\ t_6 &= 0.04; \end{aligned}$$

(2) we can bring the system of equations into the matrix form and find the unknowns using Cramer's method of solving a system of complex linear equations. First, the determinant  $\Delta$  of the matrix formed using the system of equations is found.

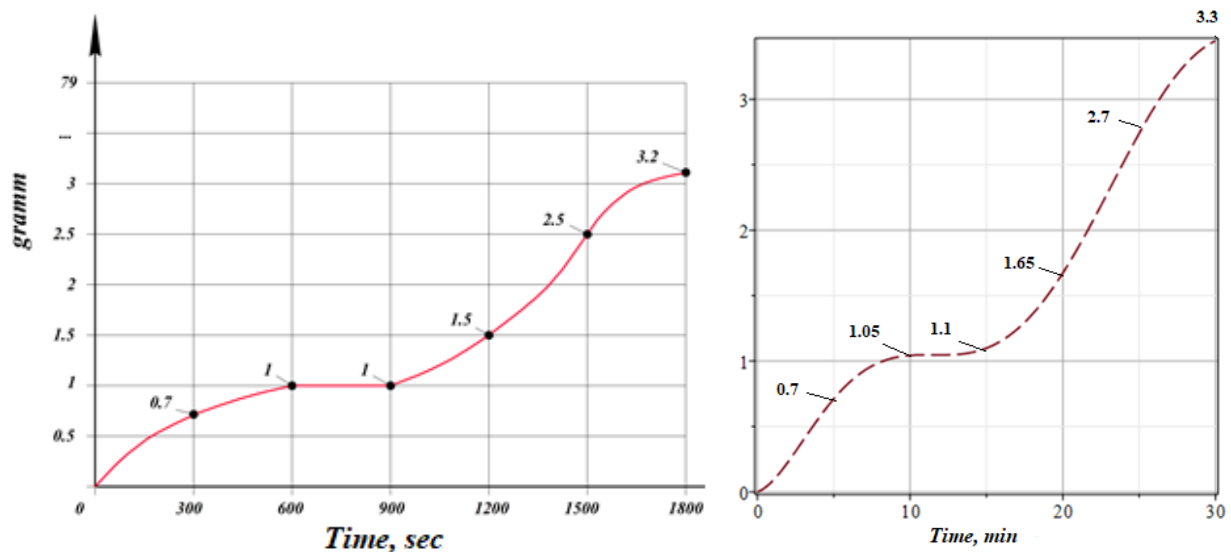
$$\Delta = \begin{vmatrix} 15625 & 3125 & 625 & 125 & 25 & 5 \\ 1000000 & 100000 & 10000 & 1000 & 100 & 10 \\ 11390625 & 759375 & 50625 & 3375 & 225 & 15 \\ 64000000 & 3200000 & 160000 & 8000 & 400 & 20 \\ 244140625 & 9765625 & 390625 & 15325 & 625 & 25 \\ 729000000 & 24300000 & 810000 & 27000 & 900 & 30 \end{vmatrix} = -1.186523437499922e+22 \quad (3)$$

solving the above matrices, we find the following values of the unknowns,

$$\begin{aligned} x_1 &= \frac{\Delta_1}{\Delta} = \frac{-15820312250000000}{-1.186523437499922e+22} = \frac{823974609375}{6179809570312094000}; \\ x_2 &= \frac{\Delta_2}{\Delta} = \frac{166113281249998200}{-1.186523437499922e+22} = -\frac{185394287109373}{13242449079240200000}; \\ x_3 &= \frac{\Delta_3}{\Delta} = \frac{-6288574218749809000}{-1.186523437499922e+22} = \frac{1535296440124465}{2896785736083794000}; \\ x_4 &= \frac{\Delta_4}{\Delta} = \frac{101052246093751120000}{-1.186523437499922e+22} = -\frac{128494575619699}{15087425708769760}; \\ x_5 &= \frac{\Delta_5}{\Delta} = \frac{-601171875000039200000}{-1.186523437499922e+22} = \frac{286661088466663}{5657784640788660}; \\ x_6 &= \frac{\Delta_6}{\Delta} = \frac{-494384765624744150000}{-1.186523437499922e+22} = \frac{235741026699421}{5657784640788660}; \end{aligned}$$

After solving the above equations and determining the unknowns, the function representing the wear resistance of low – alloyed steel alloy 35XGCL as a function of time is as follows:

$$m = (1.3 \cdot 10^{-7})t^6 - (1.4 \cdot 10^{-5})t^5 + (5.3 \cdot 10^{-4})t^4 - (8.5 \cdot 10^{-3})t^3 + 0.05t^2 + 0.04t; \quad (4)$$



**Pic 3. Mathematical model based on research results correspondence to actual results**

Next, based on the developed suggestions, we will create a mathematical model of the time dependence of the wear resistance of the sample with 0.3-0.5% Ti element added as a modifier to the alloy composition. For this, time change is taken as a free variable, and we will consider the problem of creating a function that reflects the corrosion of the alloy. In this case, we construct Lagrange's interpolation polynomial, that is, by bringing the problem into the system of algebraic equations, it is possible to express the function of the amount of consumption in the form of a polynomial by determining the unknown coefficients.

$m$  – wear resistance, gram;

$t$  – time, minute;

$$m = f(t); (5)$$

$$\begin{cases} 5^6 t_1 + 5^5 t_2 + \dots + 5t_6 = 0.3 \\ 10^6 t_1 + 10^5 t_2 + \dots + 10t_6 = 0.5 \\ 15^6 t_1 + 15^5 t_2 + \dots + 15t_6 = 0.6 \\ 20^6 t_1 + 20^5 t_2 + \dots + 20t_6 = 0.8 \\ 25^6 t_1 + 25^5 t_2 + \dots + 25t_6 = 1.5 \\ 30^6 t_1 + 30^5 t_2 + \dots + 30t_6 = 2.5 \end{cases}; \quad (6)$$

$$t_1 = -7.11 \cdot 10^{-8};$$

$$t_3 = -1.38 \cdot 10^{-4};$$

$$t_5 = -0.01;$$

$$t_2 = 5.33 \cdot 10^{-6};$$

$$t_4 = 1.6 \cdot 10^{-3};$$

$$t_6 = 0.087;$$

(6) we can bring the system of equations into the matrix form and find the unknowns using Cramer's method of solving a system of complex linear equations. First, the determinant  $\Delta$  of the matrix formed using the system of equations is found.

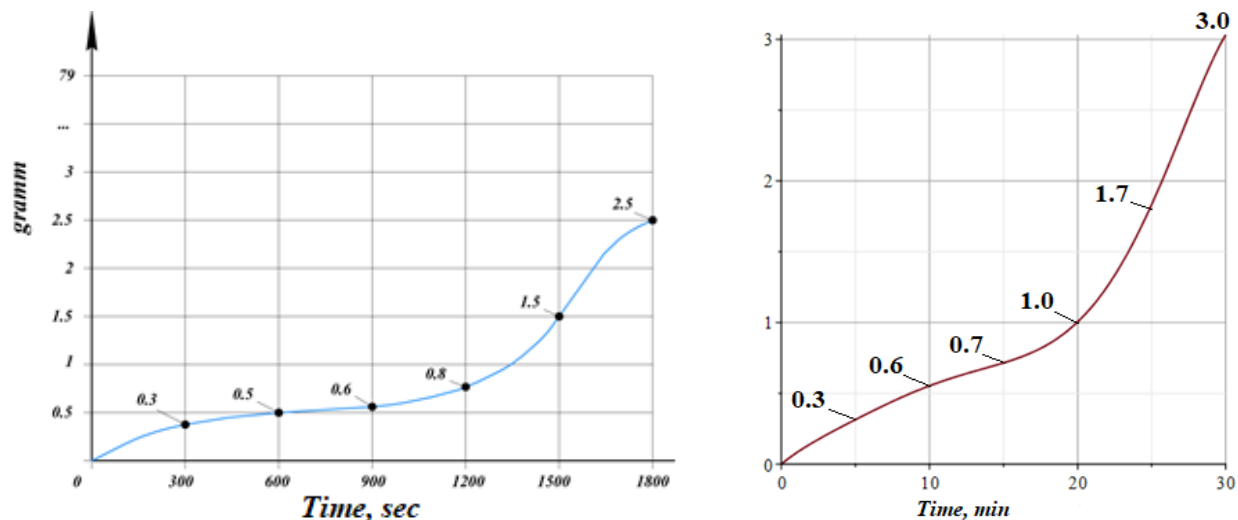
$$\Delta = \begin{vmatrix} 15625 & 3125 & 625 & 125 & 25 & 5 \\ 1000000 & 100000 & 10000 & 1000 & 100 & 10 \\ 11390625 & 759375 & 50625 & 3375 & 225 & 15 \\ 64000000 & 3200000 & 160000 & 8000 & 400 & 20 \\ 244140625 & 9765625 & 390625 & 15325 & 625 & 25 \\ 729000000 & 24300000 & 810000 & 27000 & 900 & 30 \end{vmatrix} = -1.186523437499922e+22 \quad (7)$$

solving the above matrices, we find the following values of the unknowns,

$$\begin{aligned} x_1 &= \frac{\Delta_1}{\Delta} = \frac{843750000000000}{-1.186523437499922e+22} = -\frac{164794921875}{2317428588867035000}; \\ x_2 &= \frac{\Delta_2}{\Delta} = \frac{-6328124999999940}{-1.186523437499922e+22} = \frac{988769531249999}{185394287109362800000}; \\ x_3 &= \frac{\Delta_3}{\Delta} = \frac{1634765625000033300}{-1.186523437499922e+22} = -\frac{1596450805664095}{11587142944335176000}; \\ x_4 &= \frac{\Delta_4}{\Delta} = \frac{-1898437500000233000}{-1.186523437499922e+22} = \frac{48279762268067}{30174851417539520}; \\ x_5 &= \frac{\Delta_5}{\Delta} = \frac{124716796874995530000}{-1.186523437499922e+22} = -\frac{237878412008277}{22631138563154640}; \\ x_6 &= \frac{\Delta_6}{\Delta} = \frac{-1.0283203124999335e+21}{-1.186523437499922e+22} = \frac{1961365342140071}{22631138563154640}; \end{aligned}$$

After solving the above equations and determining the unknowns, based on the proposals developed, the function representing the wear resistance of the alloy with 0.3-0.5% Ti as a modifier is as follows [5 – 12]:

$$m = -(7.11 \cdot 10^{-8})t^6 + (5.33 \cdot 10^{-6})t^5 - (1.38 \cdot 10^{-4})t^4 + (1.6 \cdot 10^{-3})t^3 + 0.01t^2 + 0.087t; \quad (8)$$



**Pic 4. Mathematical model based on research results correspondence to actual results**

**Conclusions.** Based on the results of the research, it was found that the corrosion resistance was significantly improved under the influence of the titanium element added as a modifier to the alloy composition in the amount of 0.3 - 0.5%. The results obtained based on the results of practical research



were compared with the results obtained based on mathematical models. The results are confirmed to be compatible.

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